Homotopy types of diffeomorphisms groups of simplest Morse-Bott foliations on lens spaces

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Let F be the Morse-Bott foliation on the solid torus $T = S^1 \times D^2$ into 2-tori parallel to the boundary and one singular circle $S^1 \times 0$. A diffeomorphism $h : T \to T$ is called *foliated* (resp. *leaf preserving*) if for each leaf $\omega \in F$ its image $h(\omega)$ is also leaf of F (resp. $h(\omega) = \omega$). Gluing two copies of T by some diffeomorphism between their boundaries, one gets a lens space $L_{p,q}$ with a Morse-Bott foliation $F_{p,q}$ obtained from F on each copy of T. Denote by $\mathcal{D}^{fol}(T, \partial T)$ and $\mathcal{D}^{lp}(T, \partial T)$ respectively the groups of foliated and leaf preserving diffeomorphisms of T fixed on the boundary ∂T. Similarly, let $\mathcal{D}^{fol}(L_{p,q})$ and $\mathcal{D}^{lp}(L_{p,q})$ be respectively the groups of foliated and leaf preserving diffeomorphisms of $F_{p,q}$. Endow all those groups with the corresponding C^∞ Whitney topologies. The aim of the talk is give a complete description the homotopy types of the above groups $\mathcal{D}^{fol}(T, \partial T)$, $\mathcal{D}^{lp}(T, \partial T)$, $\mathcal{D}^{fol}(L_{p,q})$, $\mathcal{D}^{lp}(L_{p,q})$ for all p, q.

References

[1] O. Khokhliuk, S. Maksymenko, *Homotopy types of diffeomorphisms groups of simplest Morse-Bott foliations on lens spaces, 1,* `arXiv:2210.11043`

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