



*International scientific online conference*

# **Algebraic and Geometric Methods of Analysis**

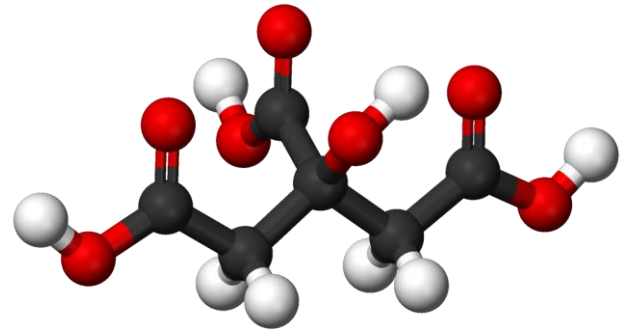
- Title: **Shape optimization in the batch crystallization of CAM**
- Author: **Enzo Bonacci (The Natural Sciences Unit of ATINER)**
- Topic: **Geometric and topological methods in natural sciences**
- Conference: **International scientific conference AGMA 2023**
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# *The state of art in 1997*

Citric acid [8] is an important organic substance but, until 1997, the scientific literature reported little information about the crystallization by cooling in stirred-tank reactors (STRs), i.e., the process by which the commercial product is obtained.

The studies then available were focused mostly on the kinetics of nucleation [13] and on the crystal growth [14] rather than on the industrial aspects of the crystallization in STRs.

**Formula:  $C_6H_8O_7$**



**Structure: monoclinic**



# *Producing CAM at La Sapienza's lab*

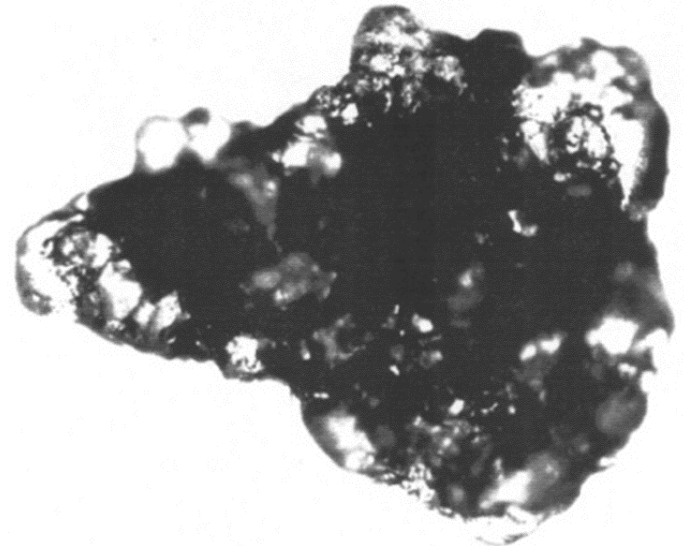
The Department of Chemical Engineering at the University "La Sapienza" of Rome decided to fill that sci-tech gap through a detailed investigation on the crystallization in discontinuous (batch) of the citric acid monohydrate (CAM) at San Pietro in Vincoli's lab (DICMA).

The author participated in that cutting edge experience, under the supervision of Prof. Barbara Mazzarotta, in the years 1997-1998.

**Crystal size 150-180  $\mu\text{m}$**



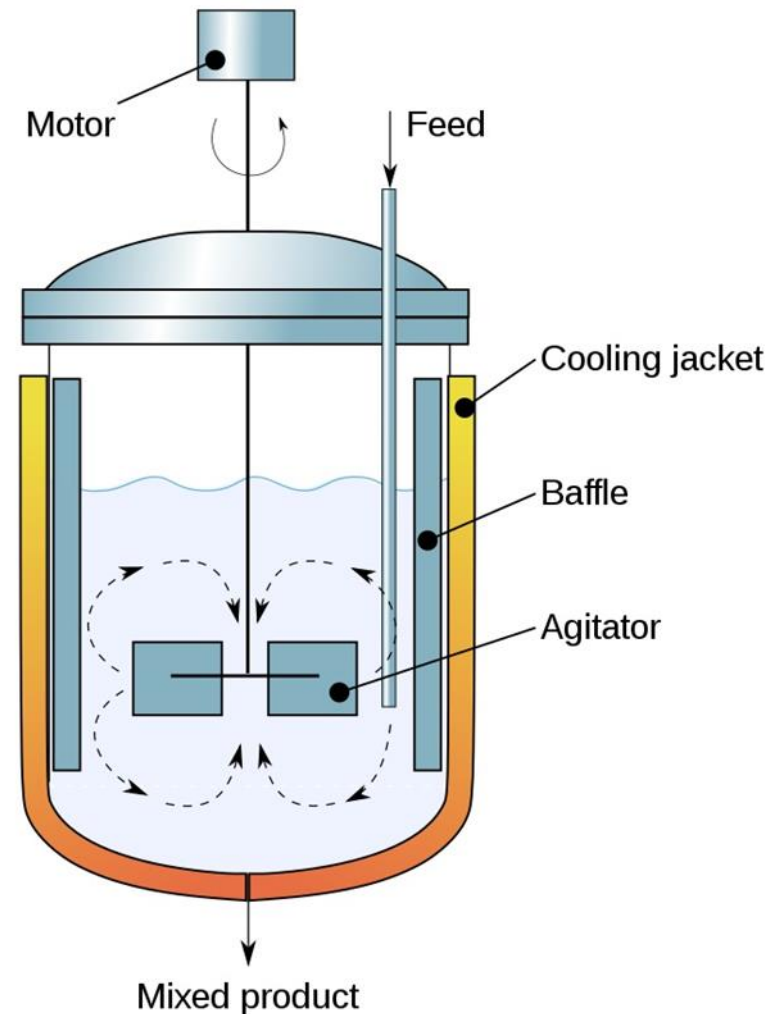
**Crystal size 1.18-1.4 mm**



# *Seeking for an optimal CSD of CAM*

We spotted the main operating conditions in batch reactors, we modified them until an *optimal* crystal size distribution (CSD) of CAM [7], confirmed also via computational fluid-dynamics (CFD), and we wrote a QBasic program predicting the outcomes of any test [6].

The resulting M.Sc. thesis [3] and the related research papers [4,5,11] were acknowledged as *pioneering* achievements more than a decade later [1,2,10,12].



# ***Finding the optimal shape of STRs***

Here we expound only the influence of the STRs' geometry.

We show that the best CSD, i.e., a homogenous distribution of large crystals, always comes from round-bottomed tanks.

Hemispherical tanks perform slightly better than conical and much better than flat (discarded in industrial practices).

Based on experimental tests and computer simulations, such conclusions seem valid beyond the limits of our survey on CAM.

**Influence on the crystallization of various factors**

**Geometry of the stirred-tank reactor's bottom**

**Experimental tests in differently shaped STRs**

**Round bottom better than conical and flat**

## *Results of a meticulous testing*

A series of 20 batch tests let us identify the operating parameters ensuring an optimal CSD of CAM.

These conditions can be summarized as follows:

1. Three-blade marine propeller as impeller.
2. Agitation speed  $\sim 2\%$  above the minimum value for solid suspension [15].
3. Seed crystals large  $\sim 10\%$  of the desired final size.
4. Seeding temperature  $\sim 0.5$  °C over that of spontaneous nucleation.
5. Tank crystallizer with a round (hemispherical) bottom.

In this talk we illustrate the last achievement, i.e., the role played by the STRs in crystallizing the CAM thanks to their differently shaped bottoms [9].

# *A strict test protocol*

All tests were executed via the following eight steps:

- 1)Preparation of an aqueous solution of citric acid in the volume of 8 L, saturated at a temperature of 25 °C, i.e., 3.39 kg of water and 7.09 kg of citric acid;
- 2)Solubilization by heating;
- 3)Crystallization by cooling: we descended from 30 °C to a final temperature between 19 °C and 20 °C, i.e., 5 °C or 6 °C lower than the saturation temperature, in order to attain the desired precipitation;
- 4)Separation by filtration *under vacuum*;
- 5)Drying on exposure to air;
- 6)Classification of the crystalline product;
- 7)Analysis through the optical microscope;
- 8)Pictures of some crystal specimens.

# Comparing our three STRs' shapes

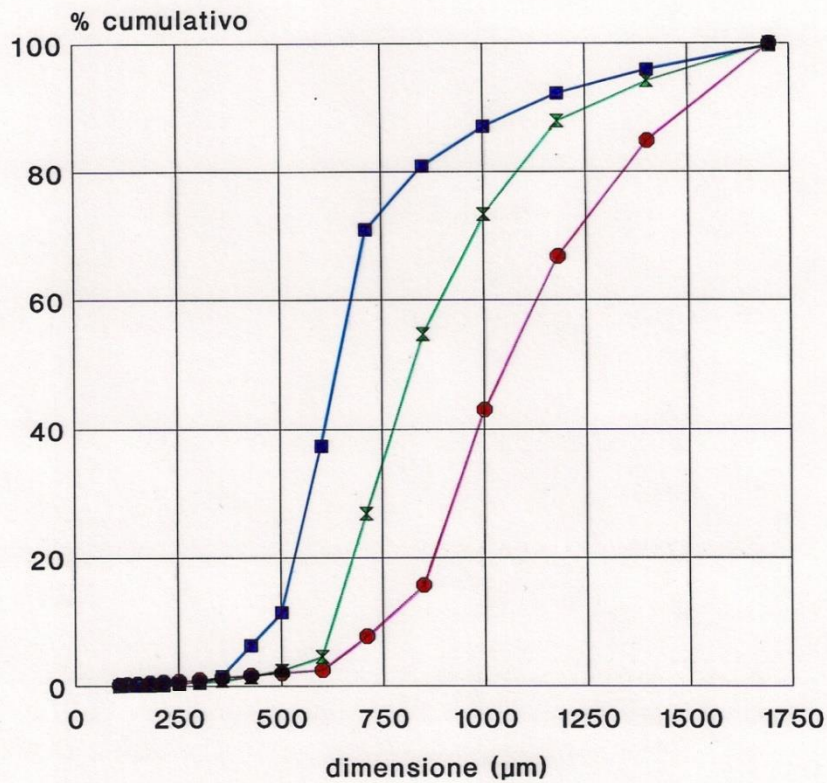
<b>Geometric features of our STRs:</b>	<b>FLAT</b>	<b>ROUND</b>	<b>CONICAL</b>
<i>TANK's volume (L):</i>	10.1	9.9	9.8
<i>TANK's total height (mm):</i>	265	350	325
<i>TANK's height of the body (mm):</i>	265	255	205
<i>TANK's height of the bottom (mm):</i>	0	95	120
<i>TANK's outer diameter (mm):</i>	230	214	230
<i>TANK's inner diameter (mm):</i>	220	204	220
<i>JACKET's height (mm):</i>	120	120	120
<i>JACKET's outer diameter (mm):</i>	270	254	270
<i>JACKET's inner diameter (mm):</i>	260	244	260
<i>JACKET's distance from the top (mm):</i>	80	100	50
<i>JACKET's distance to the bottom (mm):</i>	65	35	35
<i>BAFFLES' height (mm):</i>	260	250	200
<i>BAFFLES' width (mm):</i>	20	20	20
<i>BAFFLES' thickness (mm):</i>	5	5	5



# Comparison among tests

## Comparing our three STRs

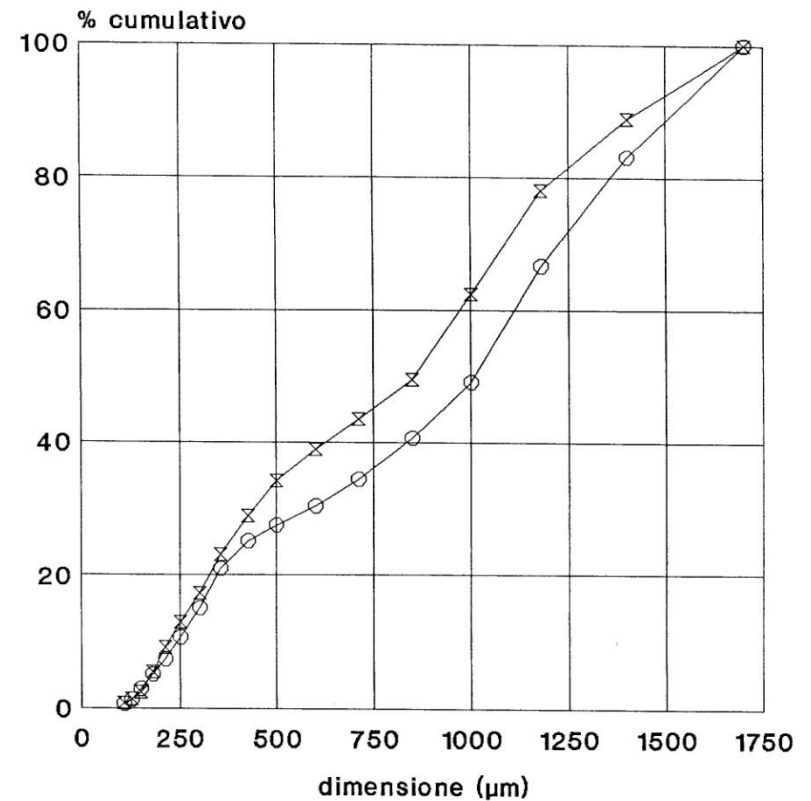
VARIAZIONE DEL TIPO DI GEOMETRIA  
sem.leggera,  $T_s=22^\circ\text{C}$ , bassa agitazione



● PROVA 8 (F.tondo)      ▲ PROVA 12 (F.conico)  
■ PROVA 14 (F.piano)

## The best two STRs

VARIAZIONE DEL TIPO DI GEOMETRIA  
sem.pesante,  $T_s=22^\circ\text{C}$ , bassa agitazione



× PROVA 9 (F.conico)      ○ PROVA 13 (F.tondo)

# *The best STRs according to our tests*

**1<sup>st</sup>) Round-bottomed STR**

**2<sup>nd</sup>) Conical-bottomed STR**



## *Interpreting our tests*

All the collected data indicated that a stirred-tank reactor with a *hemispherical bottom* was preferable to any other differently shaped STR, producing large-sized homogeneous CAM crystals. On the opposite, the flat-bottomed STR gave bad results in terms of CSD, with a high percentage of fine-grained crystals and a significantly reduced average size.

The best performance of the round-bottomed tank was surely due to its *optimal shape* and not to other parameters, such as the different thermal profile induced by the cooling jackets or the mixing efficacy.

To corroborate our conclusion, we measured the *heat exchange* in each STR: maximum for the vessel with a conical base, followed by the round and, eventually, the flat-bottomed tank.

We established also the *agitation* efficiency in each STR: maximum for the vessel with a flat base, followed by the conical and, finally, the round-bottomed tank.

# Computational fluid dynamics

The experimental evidences were supported by the VisiMix software ([www.visimix.com](http://www.visimix.com)) computing the fluid dynamics inside each crystallizer for CAM viscosity in the range  $T=19-22$  °C and for the tests' standard speed  $N_C=755$  rpm.

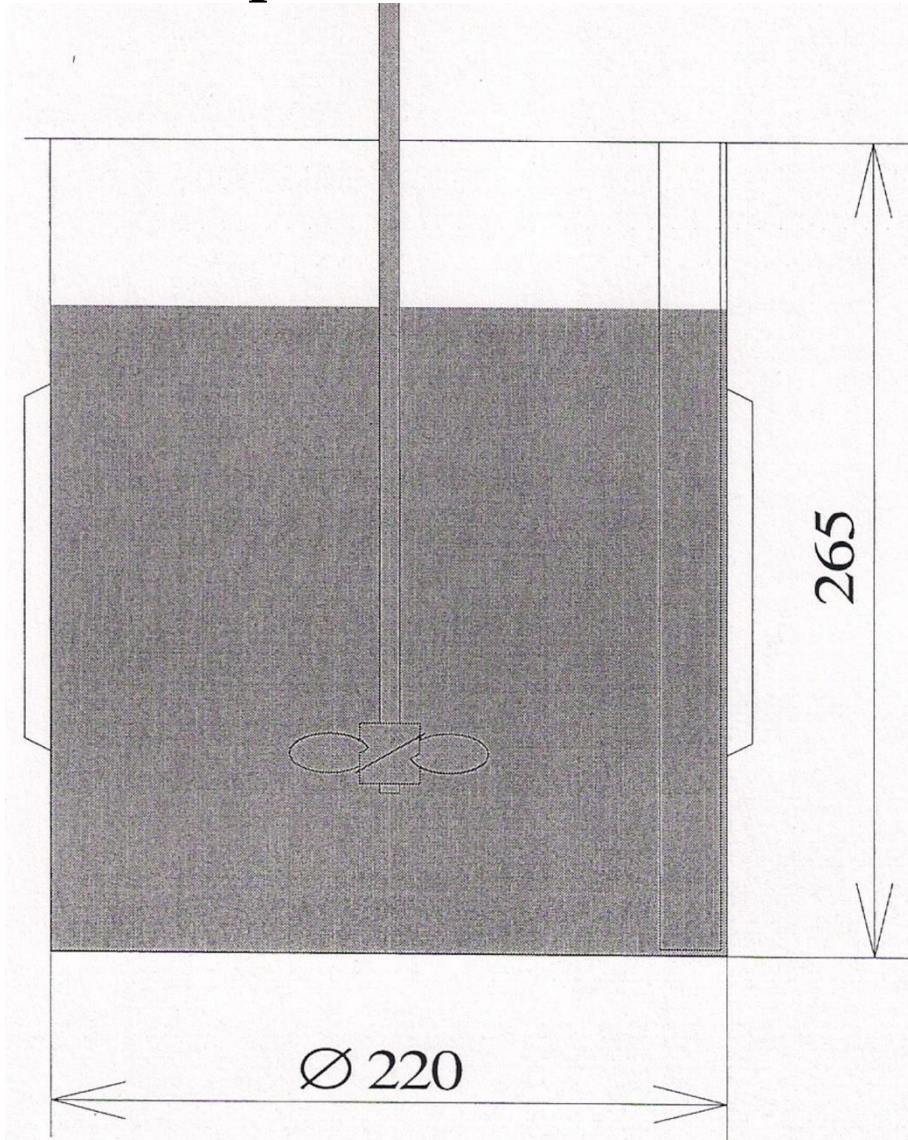
The *round* shape was confirmed as the best STR's bottom because the flux lines, constantly tangent to its inner surface, assured the best dispersion for the suspended CAM particles.

The *conical* shape did not fully comply the dispersed phase's motion lines given by the impeller, whereas the *flat-bottomed* STR's deformed flux lines generated the worst suspension state.

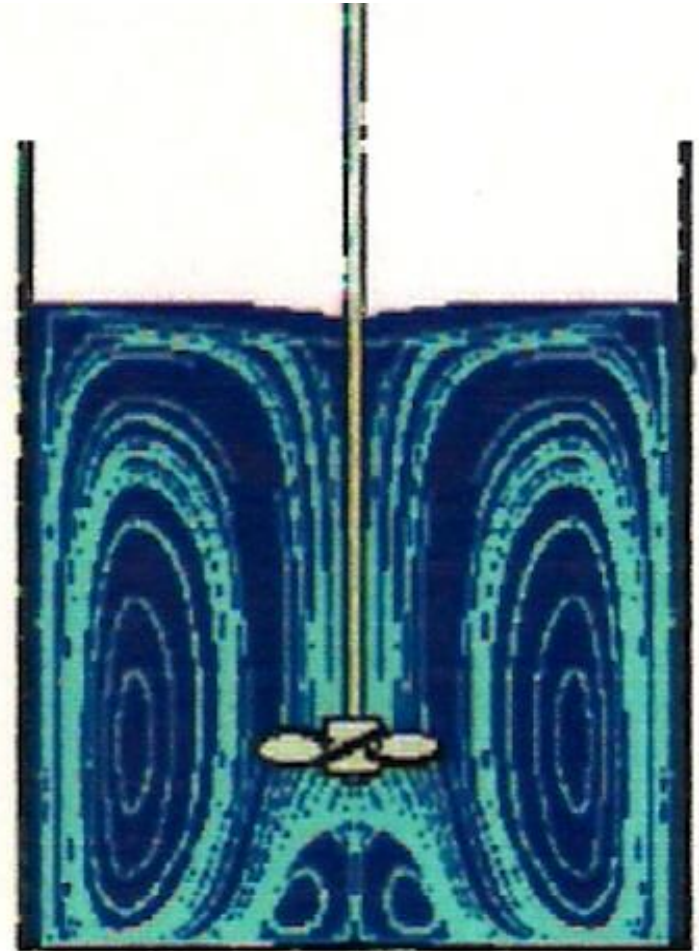
Being scarcely affected by *mixing* (choice of the impeller and/or the stirring rate) and by *viscosity* (choice of the substance and/or the temperature for the cooling process), such conclusions seem valid in general, for *any* batch crystallization.

# *The flat-bottomed crystallizer*

**A shape to be avoided**

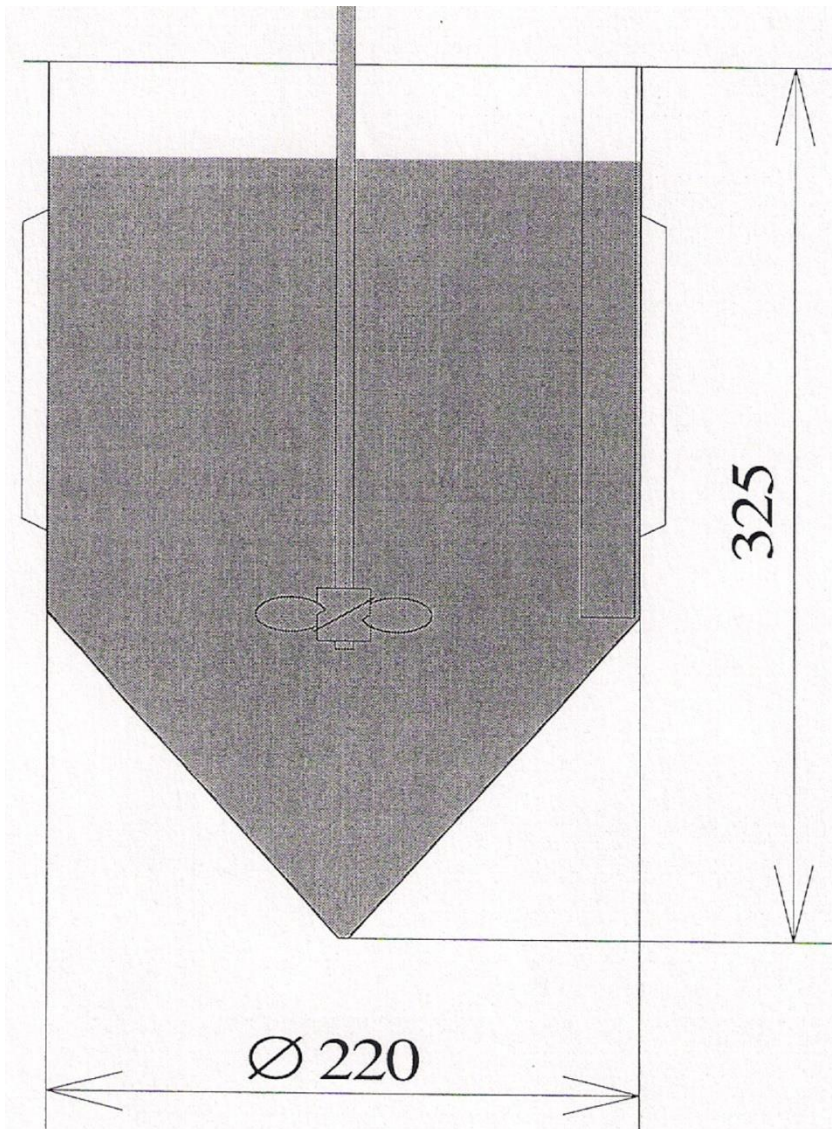


**An ineffective flux**



# *The conical-bottomed crystallizer*

**A possible shape**

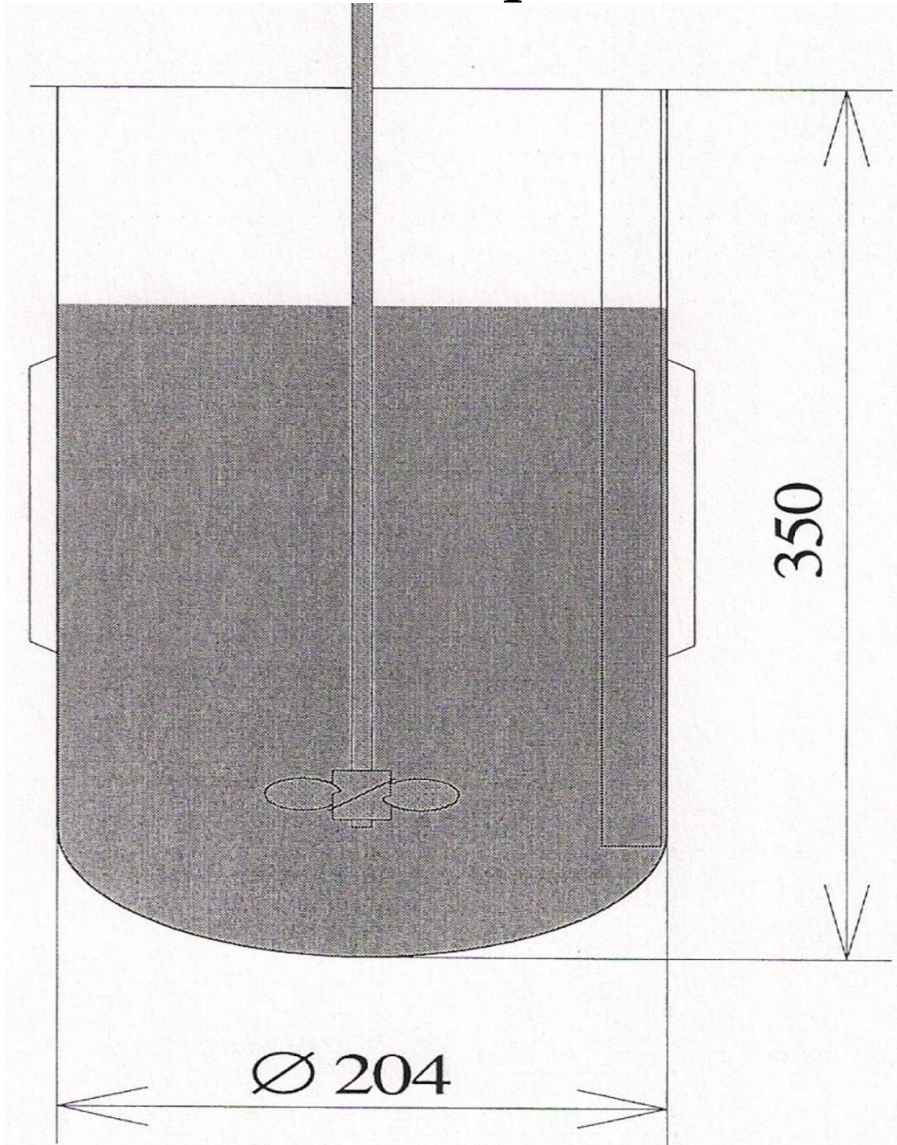


**An acceptable flux**

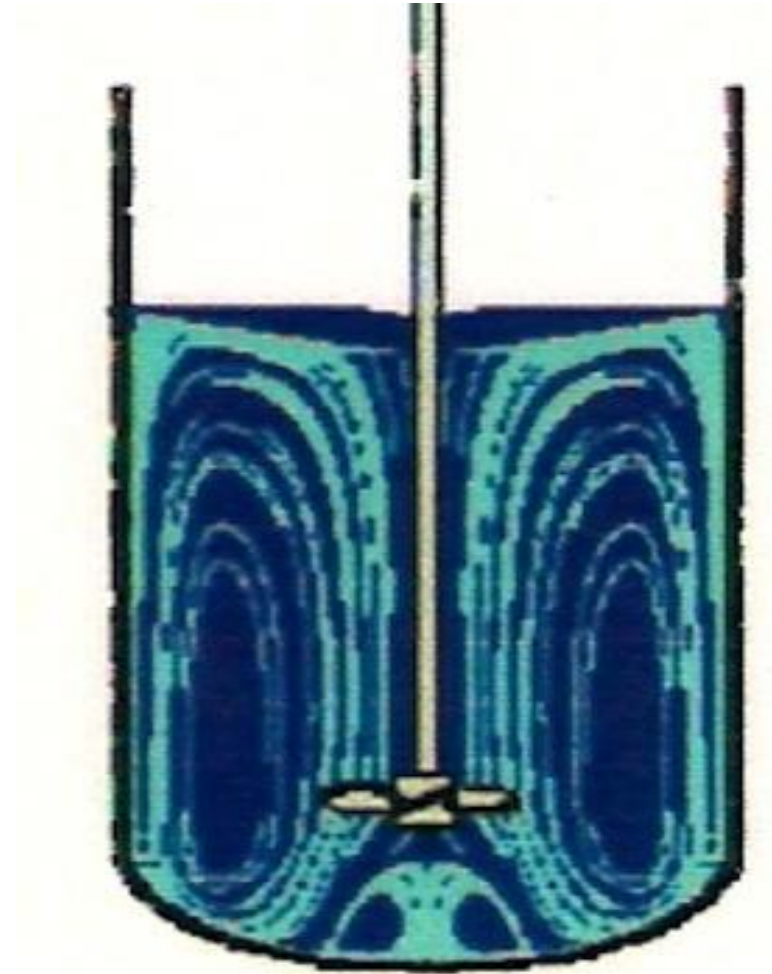


# *The round-bottomed crystallizer*

**The best shape**



**The optimal flux**



# *The best STRs according to CFD*

**Best STR  
(round bottom)**



**Second best STR  
(conical bottom)**





# *A simulation program in QBasic*

In order to simulate the CAM tests, we wrote a QBasic program *ad hoc* (see, e.g., [www.qbasic.net](http://www.qbasic.net)) starting from a previous work about the batch crystallization of the potassium sulfate.

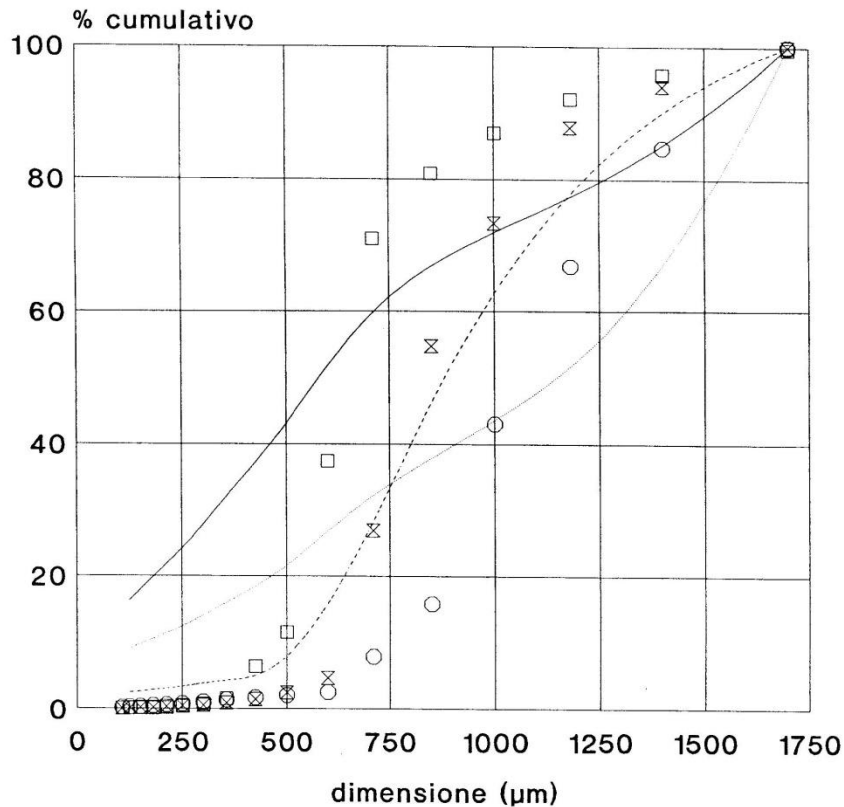
The CAM peculiarities, inferred via the microscopic analysis of its grains [8], were coded through subroutines specific for the agglomeration and the secondary nucleation by collision [6] of the discontinuous phase.

Eventually, the experimental data were in good agreement with the predictions and it was possible to reproduce faithfully the influence of the cooling profile on the crystal granulometric properties and the effects of all the operating variables, except with *heavy seed* crystals.

# Comparing simulations with real data

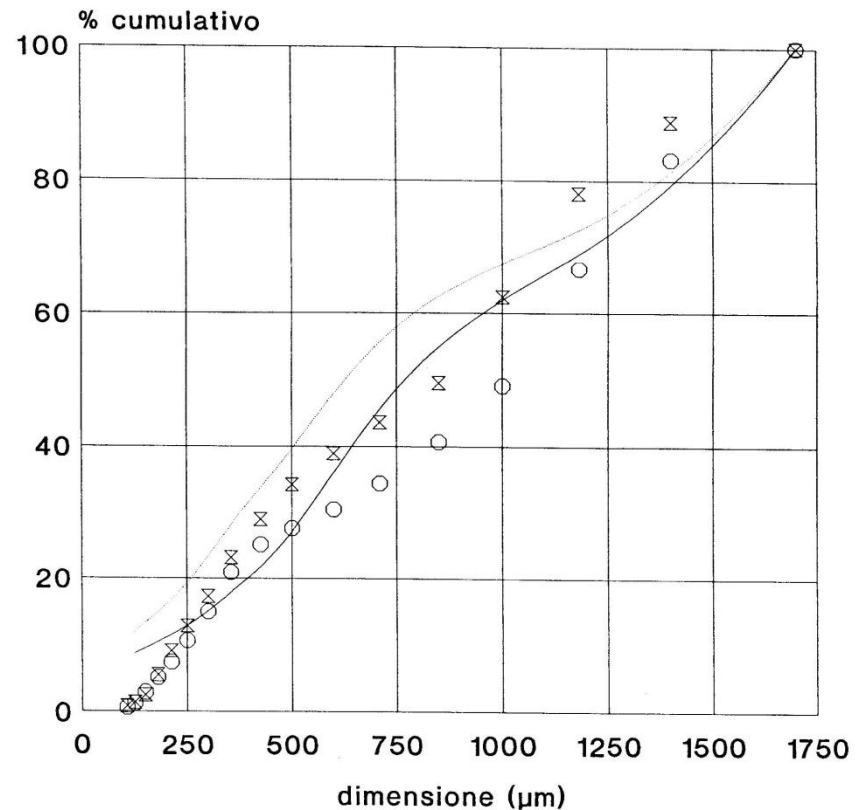
## Comparing our three STRs

VARIAZIONE DEL TIPO DI GEOMETRIA  
sem.leggera,  $T_s=22^\circ\text{C}$ , bassa agitazione



## The best two STRs

VARIAZIONE DEL TIPO DI GEOMETRIA  
sem.pesante,  $T_s=22^\circ\text{C}$ , bassa agitazione



○ PROVA 8      × PROVA 12      □ PROVA 14  
 - - - F.tondo      - - - F.conico      — F.piano

× PROVA 9      ○ PROVA 13  
 - - - F.conico      — F.bombato

# *The best STRs according to simulations*

**1<sup>st</sup>) Round-bottomed STR**



**2<sup>nd</sup>) Conical-bottomed STR**



# Conclusions

In the years 1997-1998, at La Sapienza's DICMA-lab we analyzed the batch cooling crystallization of the citric acid monohydrate (CAM) from aqueous solutions.

The choice of a stirred-tank reactor (STR) with a hemispherical bottom *optimized* the process, allowing the best suspension state for CAM particles.

Looking for a homogenous distribution of large crystals, we found that the conical-bottomed STR was in second place for efficiency, whereas the flat-bottom shape performed rather poorly, providing the lowest crystalline quality.

The experimental work was supplemented by a QBasic program to predict the CSD and by the VisiMix software to simulate the fluid dynamics inside each crystallizer.

# *Acknowledgements*

As far as the study on CAM is concerned, we wish to thank the Organizing and Scientific Committees of the:

- *SIF 96<sup>th</sup> Congress in Bologna*, for the 2010 talk **[1]**;
- *International Year of Chemistry*, for the 2011 lecture **[2]**;
- *Magna Graecia 15<sup>th</sup> Prize*, for the 2012 Science Award;
- *Sapio Prize*, for the 2012-2018 award nominations;
- *Aracne Editrice*, for the 2013 “Diritto di Stampa” **[3]**;
- *SIF 101<sup>st</sup> Congress in Rome*, for the 2015 talk **[9]**;
- *Ettore Majorana 40<sup>th</sup> Gran Gala*, for the 2015 invitation;
- *ICMCS 5<sup>th</sup> Conference*, for the 2016 appreciation **[10]**;
- *Frascati Scienza*, for the ERN 2019 invited lecture **[12]**;
- *AGMA 7<sup>th</sup> Conference in Odesa*, for the 2023 talk.

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- 1) E. Bonacci.** Experimental Survey on the Batch Crystallization of CAM. In: Proceedings of the 96th National Congress of the Italian Physical Society, Bologna (Sept. 20-24, 2010), Atticon5594.
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- 3) E. Bonacci.** Studio sperimentale sulla cristallizzazione dell'acido citrico. Vol. 40 of Diritto di Stampa. Rome, Aracne Editrice, 2013 (ISBN 9788854857674).
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- 15) N.T. Zwietering.** Suspending of Solid Particles in Liquid by Agitators. *Chem. Eng. Sci.* Vol.8 No.3–4 (1958) 244–253.



# *Image credits*

## **Slide 1.**

[www.imath.kiev.ua/~topology/conf/agma2018/images/bg.jpg](http://www.imath.kiev.ua/~topology/conf/agma2018/images/bg.jpg)

## **Slide 2.**

[https://en.wikipedia.org/wiki/Citric\\_acid#/media/File:Citric-acid-3D-balls.png](https://en.wikipedia.org/wiki/Citric_acid#/media/File:Citric-acid-3D-balls.png)

[https://en.wikipedia.org/wiki/Citric\\_acid#/media/File:Zitronens%C3%A4ure\\_Kristallzucht.jpg](https://en.wikipedia.org/wiki/Citric_acid#/media/File:Zitronens%C3%A4ure_Kristallzucht.jpg)

## **Slide 3.**

[www.researchgate.net/publication/279193084\\_Photo\\_gallery\\_of\\_CAM\\_crystals\\_from\\_aqueous\\_solutions](http://www.researchgate.net/publication/279193084_Photo_gallery_of_CAM_crystals_from_aqueous_solutions)

## **Slide 4.**

[https://en.wikipedia.org/wiki/Baffle\\_\(heat\\_transfer\)#/media/File:Agitated\\_vessel.svg](https://en.wikipedia.org/wiki/Baffle_(heat_transfer)#/media/File:Agitated_vessel.svg)