CHAIN-REGULAR AND REGULAR COMPONENTS OF THE WANDERING SET OF SURFACE HOMEOMPRPHISMS

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Regular components of the wandering set of surface homeomorphisms were introduced by Birkgoff [1, 2]. With the emergence of the chain recurrent set theory introduced by Conley [3] for flows and adapted for discrete dynamical systems by Franks and Hurley [4, 5] we can define an analog of regular components of the wandering set for the set of chain-regular points (points that are not chain recurrent) as the set of points that divide an attractor-repeller pair.

We study the topology of chain-regular components of surface homeomorphisms and show that it is in fact different from the topology of regular components of the wandering set.

References

- [1] G. Birkhoff. Dynamical systems. Colloquium Publications. V. 9, AMS, Providence, RI, 1927.
- [2] G. Birkhoff, P. Smith. Structure analysis of surface transformations. J. Math, 7:357–369, 1928.
- [3] Charles Conley. Isolated invariant sets and the Morse index, volume 38 of CBMS Regional Conference Series in Mathematics. American Mathematical Society, Providence, R.I., 1978.
- [4] John Franks. A variation on the Poincaré-Birkhoff theorem, volume 81 of Contemp. Math., pages 111–117. Amer. Math. Soc., Providence, RI, 1988.
- [5] Mike Hurley. Chain recurrence, semiflows, and gradients. J. Dynam. Differential Equations, 7(3):437–456, 1995.