

International scientific online conference

# Algebraic and geometric methods of analysis

May 26-29, 2025, Ukraine

**Title: Seeding optimization in the batch crystallization of CAM**

**Author: Enzo Bonacci (The Natural Sciences Unit of ATINER)**

**Topic: Geometric and topological methods in natural sciences**

**Organizers: N. Konovenko – Y. Fedchenko – B. Feshchenko  
S. Maksymenko – O. Prishlyak**

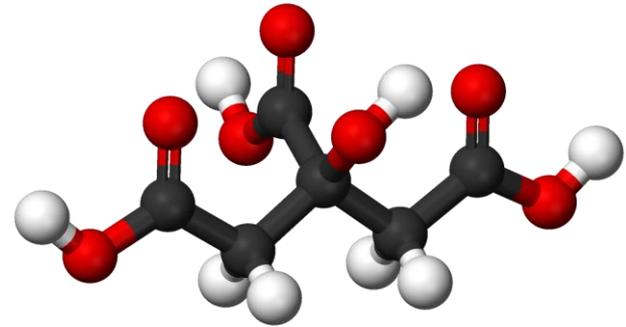
**DOI: <https://doi.org/10.13140/RG.2.2.10135.48806>**

# *The state of art in 1997*

Citric acid [8] is an important organic substance but, until 1997, the scientific literature reported little information about the crystallization by cooling in stirred-tank reactors (STRs), i.e., the process by which the commercial product is obtained.

The studies then available were focused mostly on the kinetics of nucleation [15] and on the crystal growth [16] rather than on the industrial aspects of the crystallization in STRs.

**Formula: C<sub>6</sub>H<sub>8</sub>O<sub>7</sub>**



**Structure: monoclinic**



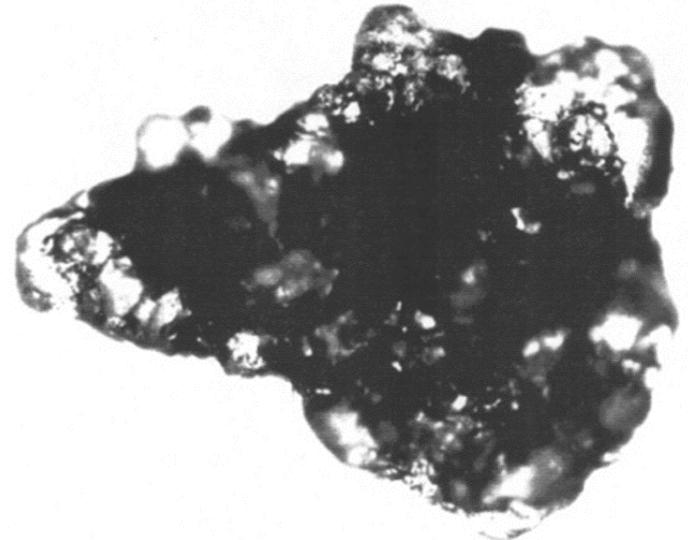
# *Producing CAM at La Sapienza's lab*

The Department of Chemical Engineering at the University “La Sapienza” of Rome decided to fill that sci-tech gap through a detailed investigation on the crystallization in discontinuous (batch) of the citric acid monohydrate (CAM) at San Pietro in Vincoli's lab (DICMA). The author participated in that cutting edge experience, under the supervision of Prof. Barbara Mazzarotta, in the years 1997-1998.

**Crystal size 150-180  $\mu\text{m}$**



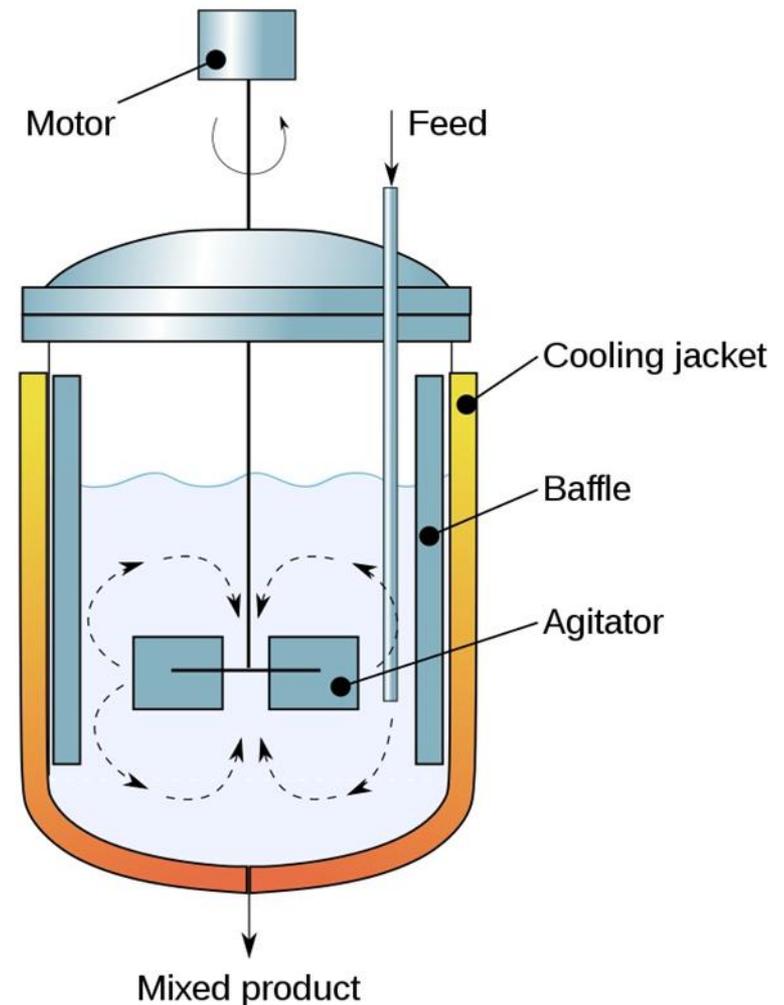
**Crystal size 1.18-1.4 mm**



# *Seeking for an optimal CSD of CAM*

We spotted the main operating conditions in batch reactors, we modified them until an *optimal* crystal size distribution (CSD) of CAM [7], confirmed also via computational fluid-dynamics (CFD), and we wrote a QBasic program predicting the outcomes of any test [6].

The resulting M.Sc. thesis [3] and the related research papers [4,5,11] were acknowledged as *pioneering* achievements more than a decade later [1,2,10,12].



## *A strict test protocol*

All tests were executed via the following eight steps:

- 1) Preparation of an aqueous solution of citric acid in the volume of 8 L, saturated at a temperature of 25 °C, i.e., 3.39 kg of water and 7.09 kg of citric acid;
- 2) Solubilization by heating;
- 3) Crystallization by cooling: we descended from 30 °C to a final temperature between 19 °C and 20 °C, i.e., 5 °C or 6 °C lower than the saturation temperature, to attain the desired precipitation;
- 4) Separation by filtration *under vacuum*;
- 5) Drying on exposure to air;
- 6) Classification of the crystalline product;
- 7) Analysis through the optical microscope;
- 8) Pictures of some crystal specimens.

# *The best STR geometry*

The optimal STR's bottom has a *round* shape because the flux lines, constantly tangent to its inner surface, assure the best dispersion for the suspended CAM particles [5,9,13].

Being scarcely affected by other factors (e.g., the *mixing* and the *viscosity*), this geometric result seems valid in general, for *any* batch crystallization.

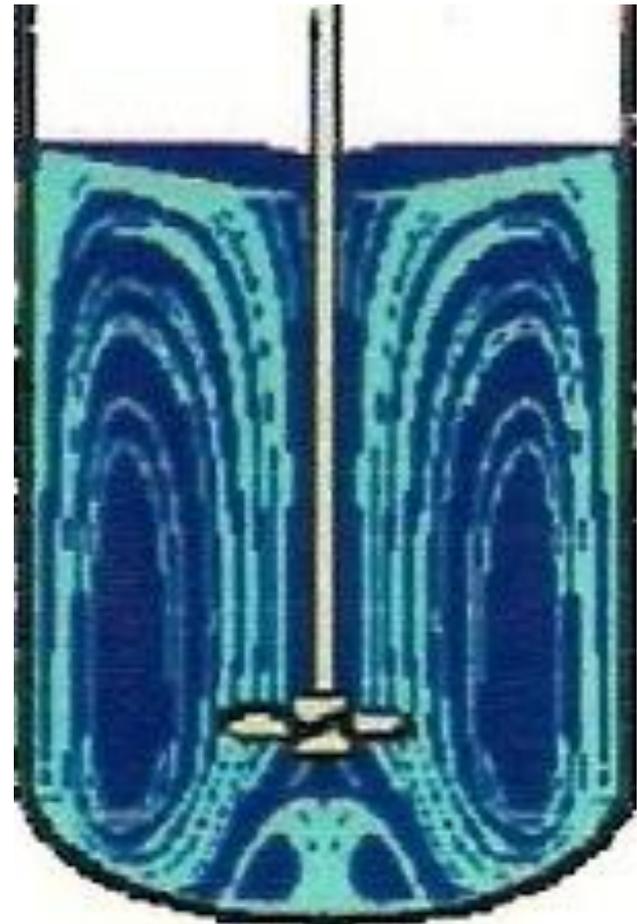


# *The best STR mixing*

The optimal mixing is in a baffled STR with a three-blade marine impeller (axial flow) at an agitation speed  $\sim 2\%$  above the minimum value for solid suspension [10,11,14].

The *VisiMix* software, computing the fluid dynamics of the low viscosity aqueous solution of citric acid inside a vertical round-bottomed small batch crystallizer, corroborates the choice of a 3-blade marine impeller.

**Best simulated flux lines**



# *The best seeding conditions*

A series of 20 batch tests let us identify the operating parameters ensuring an optimal CSD of CAM.

These conditions can be summarized as follows:

1. Three-blade marine propeller as agitator.
2. Agitation speed ~2% above the minimum value for solid suspension.
3. Seed crystals large ~10% of the desired final size.
4. Seeding temperature ~0.5 °C over that of spontaneous nucleation.
5. Tank crystallizer with a round (hemispherical) bottom.

Here we illustrate the second and third achievement, i.e., the role of the *seed crystal size & seeding temperature*.

# *Finding the optimal seeding*

In this talk we expound only the influence of the seeding.

We show that the best CSD, i.e., a homogeneous distribution of large crystals, comes from *small* size seed and *low* seeding temperature.

Namely, the seed crystals should be large one tenth of the desired CAM final average size and the seeding temperature slightly above that of spontaneous nucleation.

Such conclusions are supported by experimental tests and computer simulations.

**Influence on the crystallization of various factors**

**Dipping CAM crystal seed**

**Tests at varying temperatures and sizes of the seed**

**Light seed and low seeding temperature**

## *The optimal seeding temperature*

Experimental evidence has indicated that seeding at a *low* temperature, but *before* nucleation occurred, results in a marked improvement in the crystalline product.

The optimal temperature for seeding crystalline germs is right next to the spontaneous nucleation temperature ( $T \approx 22^\circ\text{C}$ ); the further away from this threshold, the worse it is [**1–4,6,7,12**].

However, it makes no sense to dip seed crystals once nucleation has already taken place, which is why the tests performed in this manner were stopped at an early stage.

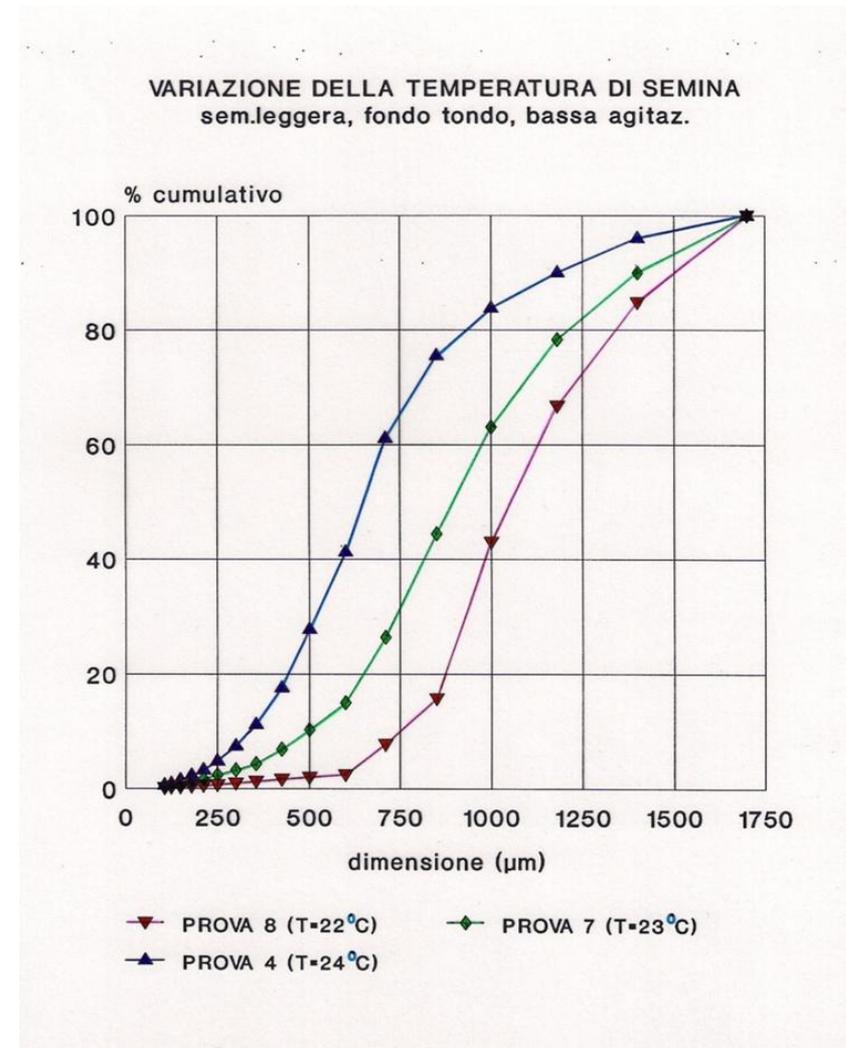
# Temperature choice from the CSD

Three successive seeding temperatures were tested: **22°C**, **23°C**, and **24°C**.

The best product was obtained at the lowest temperature (**T=22°C**), while the worst result was obtained at the highest temperature (**T=24°C**).

The optimum value of 22°C is the lower integer limit before spontaneous nucleation (between 21.4°C and 21.7°C).

## Low temperature (T=22°C)



## *Interpreting our temperature tests*

The effect of seeding is stronger as the closer the dipping of germination crystals is to the spontaneous nucleation wave (standard  $T=22^{\circ}\text{C}$ ).

In fact, if the seed is added at too high a temperature, its presence shifts the delicate meta-equilibrium, accelerating its end.

Therefore, the nucleation wave would occur at a higher thermal level (with a low initial supersaturation and a tiny remaining seed) originating a worse crystalline product, affected by a wide granulometric distribution, poor homogeneity, and small average size.

## *The optimal seed crystals' size*

Seeding always has a positive effect but, among the different types of seed, the *light* one ( $L_{\text{seed}} \approx 1/10 L_{\text{product}}$ ) is better than the heavy one ( $L_{\text{seed}} \approx 1/3 L_{\text{product}}$ ) which, in turn, is more effective than the heavier one ( $L_{\text{seed}} \approx 1/2 L_{\text{product}}$ ).

The risk of a ruinous second wave of nucleation increases with the *heaviness* of the seed.

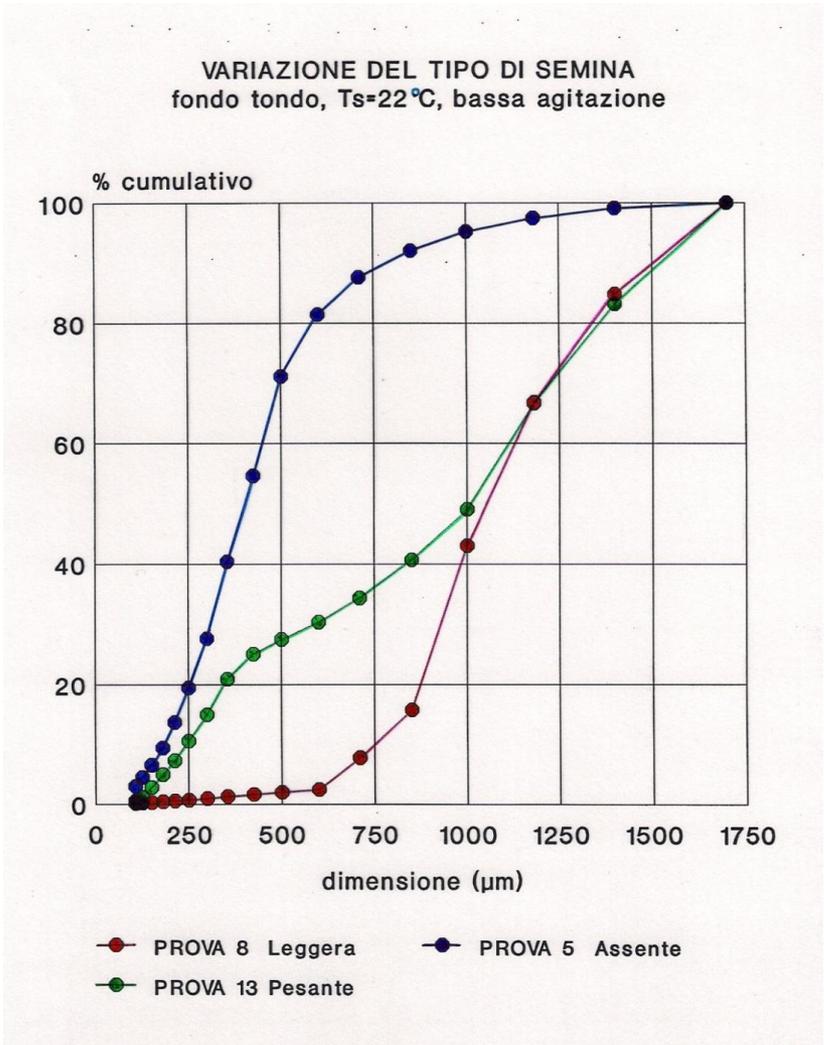
Furthermore, during growth the heavy seed crystals (with a low surface/volume ratio) are disadvantaged in energy supply, in favor of smaller crystalline conformations, and this penalizes the final average size of the distribution **[1–4,6,7,12]**.

# Size choice from the CSD

The *heavy seed's* diagram is worse than the CSD obtained with *light seed* but, in any case, better than the test in *absence of seed*, which produces tiny crystals.

The duration and intensity of any subsequent nucleation, to be avoided, would be directly proportional to the quantity and average size of the seed crystals.

Light seed ( $L_{\text{seed}} \approx 1/10 L_{\text{product}}$ )



## *Interpreting our size tests*

A *light* seed is optimal because, during the first nucleation, it removes only a minimal part of the supersaturation and, in the competitive mechanism of growth, *small* seed crystals (with a big surface/volume ratio) absorb a considerable share of the residual *driving force* (i.e., the difference between the solute's chemical potentials in, respectively, the supersaturated and saturated solution) increasing the average size of the product and avoiding further nucleation.

On the contrary, a *heavy seed* diverts a significant portion of the available supersaturation for its own growth (inhibiting the generation of other crystals), and the residual *driving force* is excessive, with an elevated risk of subsequent nucleation.

# *A simulation program in QBasic*

In order to simulate the CAM tests, we wrote a QBasic program *ad hoc* (see, e.g., [www.qbasic.net](http://www.qbasic.net)) starting from previous work about the batch crystallization of potassium sulfate.

The CAM peculiarities, inferred via the microscopic analysis of its grains [8], were coded through subroutines specific to the agglomeration and the secondary nucleation by collision [6] of the discontinuous phase.

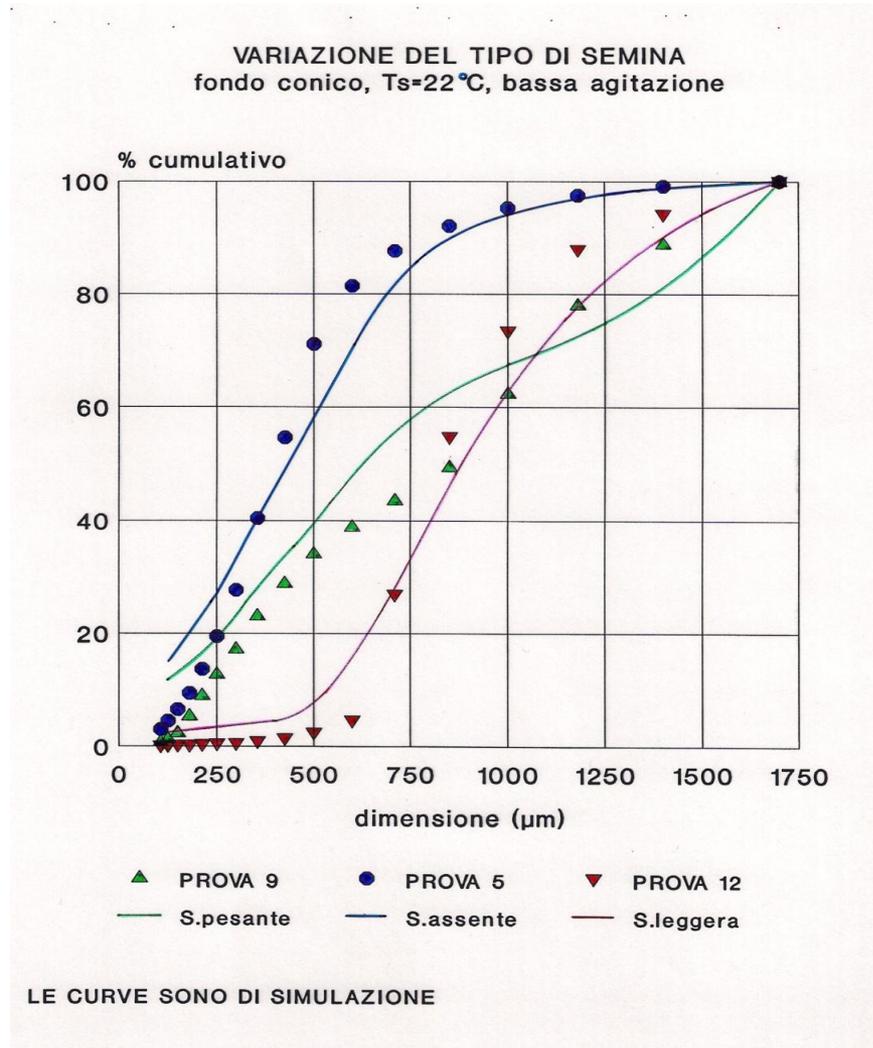
Eventually, the experimental data were in good agreement with the predictions and it was possible to reproduce faithfully the influence of the cooling profile on the crystal granulometric properties and the effects of all the operating variables, except with *heavy seed* crystals.

# Data & simulations for the conical tank

## Conical-bottomed STR



## Simulation curves



# Conclusions

In the years 1997-1998, at DICMA-lab of La Sapienza University we analyzed the batch cooling crystallization of the citric acid monohydrate (CAM) from aqueous solutions.

The choice of a *light* seed optimized the process, by avoiding subsequent nucleation and increasing the average size of the crystalline product.

Looking for a homogeneous distribution of large crystals, we found that a temperature slightly above the spontaneous nucleation ( $T=21.4^{\circ}\text{C}-21.7^{\circ}\text{C}$ ), namely  $T=22^{\circ}\text{C}$ , was the most effective to reduce the negative incidences of a low initial supersaturation and a negligible surplus seed.

The experimental work was supplemented by a QBasic program to predict the CSD.

# *Acknowledgements*

As far as the study on CAM is concerned, we wish to thank the Organizing and Scientific Committees of the:

- *SIF 96<sup>th</sup> Congress in Bologna*, for the 2010 talk [**1**];
- *International Year of Chemistry*, for the 2011 lecture [**2**];
- *Magna Graecia 15<sup>th</sup> Prize*, for the 2012 Science Award;
- *Sapio Prize*, for the 2012-2018 award nominations;
- *Aracne Editrice*, for the 2013 “Diritto di Stampa” [**3**];
- *SIF 101<sup>st</sup> Congress in Rome*, for the 2015 talk [**9**];
- *Ettore Majorana 40<sup>th</sup> Gran Gala*, for the 2015 invitation;
- *ICMCS 5<sup>th</sup> Conference*, for the 2016 appreciation [**10**];
- *Frascati Scienza*, for the ERN 2019 invited lecture [**12**];
- *AGMA 7<sup>th</sup> Conference in Odesa*, for the 2023 talk [**13**];
- *AGMA 8<sup>th</sup> Conference in Odesa*, for the 2024 talk [**14**];
- *AGMA 9<sup>th</sup> Conference in Odesa*, for the 2025 talk.

# *References*

- 1) **E. Bonacci.** Experimental Survey on the Batch Crystallization of CAM. In: Proceedings of the 96th National Congress of the Italian Physical Society, Bologna (Sept. 20-24, 2010), Atticon5594.
- 2) **E. Bonacci.** Studio sperimentale sulla cristallizzazione in discontinuo dell'acido citrico monoidrato. In: Proceedings of the International Year of Chemistry (IYC 2011) – Province of Latina. DOI: 10.13140/RG.2.1.1812.1761.
- 3) **E. Bonacci.** Studio sperimentale sulla cristallizzazione dell'acido citrico. Vol. 40 of Diritto di Stampa. Rome, Aracne Editrice, 2013 (ISBN 9788854857674).
- 4) **E. Bonacci.** A Pioneering Experimental Study on the Batch Crystallization of the Citric Acid Monohydrate. Journal of Chemistry and Chemical Engineering Vol.8 No.6 (2014) 611–620.
- 5) **E. Bonacci.** The Geometry Effect in a Pioneering Experimental Study on the Batch Crystallization of the CAM. Journal of Chemistry and Chemical Engineering Vol.8 No.7 (2014) 727–735.
- 6) **E. Bonacci.** QB Program Simulating the Batch Crystallization of the CAM. RG Dataset (2015). DOI: 10.13140/RG.2.1.3082.7683.

# *References*

- 7) **E. Bonacci.** Summary of the Findings About the Batch Crystallization of the CAM. ResearchGate Dataset (2015). DOI: 10.13140/RG.2.1.2646.6409.
- 8) **E. Bonacci.** Photo Gallery of CAM Crystals from Aqueous Solutions. RG Dataset (2015). DOI: 10.13140/RG.2.1.2673.2647.
- 9) **E. Bonacci.** The Geometry Effects on the Batch Crystallization of the CAM. In: Proceedings of the 101st National Congress of the Italian Physical Society, Rome (Sept. 21-25, 2015), Atticon8991. DOI: 10.13140/RG.2.1.1868.0806.
- 10) **E. Bonacci.** The Agitation Effects on the Batch Crystallization of the CAM. In: Proceedings of the 5th International Conference on Mathematical and Computational Sciences (V ICMCS), Thailand (Nov. 11, 2016). DOI: 10.13140/RG.2.2.30093.95205.
- 11) **E. Bonacci.** The Agitation Effects on the Batch Crystallization of the CAM. International Journal of Mathematical Sciences & Applications Vol.7 No.1 (2017) 65–71.
- 12) **E. Bonacci.** Cristallizzazione dell'Acido Citrico. In: Proceedings of the 14th European Researchers' Night (ERN 2019) – Frascati Scienza, Terra Pontina Museum (Sept. 27, 2019). DOI: 10.13140/RG.2.2.13683.68641.

# References

- 13) E. Bonacci.** Shape optimization in the batch crystallization of CAM. In: Proceedings of the 7th international scientific online conference “Algebraic and geometric methods of analysis” (AGMA 2023) – Odesa, Ukraine (May 29 – June 1, 2023). DOI: 10.13140/RG.2.2.30299.95522.
- 14) E. Bonacci.** Mixing optimization in the batch crystallization of CAM. In: Proceedings of the 8th international scientific online conference “Algebraic and geometric methods of analysis” (AGMA 2024) – Odesa, Ukraine (May 27–30, 2024). DOI: 10.13140/RG.2.2.31891.49443.
- 15) M. Bravi, B. Mazzarotta.** Primary Nucleation of Citric Acid Monohydrate: Influence of Selected Impurities. *Chemical Engineering Journal* Vol.70 No.3 (1998) 197–202.
- 16) M. Bravi, B. Mazzarotta.** Size Dependency of Citric Acid Monohydrate Growth Kinetics. *Chemical Engineering Journal* Vol.70 No.3 (1998) 203–207.

# *Image credits*

## **Slide 1.**

[www.imath.kiev.ua/~topology/conf/agma2025/assets/images/agma\\_bg.jpg](http://www.imath.kiev.ua/~topology/conf/agma2025/assets/images/agma_bg.jpg)

## **Slide 2.**

[https://en.wikipedia.org/wiki/Citric\\_acid#/media/File:Citric-acid-3D-balls.png](https://en.wikipedia.org/wiki/Citric_acid#/media/File:Citric-acid-3D-balls.png)

[https://en.wikipedia.org/wiki/Citric\\_acid#/media/File:Zitronens%C3%A4ure\\_Kristallzucht.jpg](https://en.wikipedia.org/wiki/Citric_acid#/media/File:Zitronens%C3%A4ure_Kristallzucht.jpg)

## **Slide 3.**

[www.researchgate.net/publication/279193084\\_Photo\\_gallery\\_of\\_CAM\\_crystals\\_from\\_aqueous\\_solutions](http://www.researchgate.net/publication/279193084_Photo_gallery_of_CAM_crystals_from_aqueous_solutions)

## **Slide 4.**

[https://en.wikipedia.org/wiki/Baffle\\_\(heat\\_transfer\)#/media/File:Agitated\\_vessel.svg](https://en.wikipedia.org/wiki/Baffle_(heat_transfer)#/media/File:Agitated_vessel.svg)